

# Normal Forms

Ramakrishnan & Gehrke, Chapter 17 & 18

# The Evils of Redundancy

| Dept_id | budget | Emp_id | Emp_name      | salary |
|---------|--------|--------|---------------|--------|
| 1       | 100    | 1      | John Williams | 60     |
| 1       | 100    | 2      | Phil Coulter  | 50     |
| 2       | 200    | 3      | Norah Jones   | 45     |
| 3       | 300    | 4      | Anastacia     | 40     |

- **Redundancy** at the root of several relational schema problems
  - redundant storage, insert/delete/update anomalies
- **Integrity constraints** identify problems and suggest refinements
  - in particular: functional dependencies

# Functional Dependencies

- Let  $R$  be relation,  $X$  and  $Y$  sets of attributes of  $R$
- Functional dependency (FD)**  $X \rightarrow Y$  holds over relation  $R$

if, for every allowable instance  $r$  of  $R$ :

- $t1 \in r, t2 \in r$ :  
 $\pi_X(t1) = \pi_X(t2) \implies \pi_Y(t1) = \pi_Y(t2)$
- FDs in example?

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- $K$  is a **candidate key** for  $R$  means that  $K \rightarrow R$ 
  - $K \rightarrow R$  does not require  $K$  to be minimal!
- FD is a statement about **all** allowable relation instances
  - Must be identified **based on semantics** of application
  - Given some allowable instance  $r1$  of  $R$ ,  
 we **can check if it violates** some FD  $f$ , but we **cannot tell if  $f$  holds** over  $R$ !

# Example: Constraints on Entity Set

- Consider relation obtained from Hourly\_Emps:
  - Hourly\_Emps (ssn, name, lot, rating, hrly\_wages, hrs\_worked)
- **Notation:** relation schema by listing the attributes: SNLRWH
  - **set** of attributes {S,N,L,R,W,H}
  - Using equivalently to relation name (e.g., Hourly\_Emps for SNLRWH)
- Some FDs on Hourly\_Emps:
  - ssn is key:  $S \rightarrow \text{SNLRWH}$
  - rating determines hrly\_wages:  $R \rightarrow W$

# Example (Contd.)

- Problems due to  $R \rightarrow W$  :
  - **Update anomaly:**  
change W in just the 1st tuple of SNLRWH?
  - **Insertion anomaly:**  
insert employee and don't know the hourly wage for his rating?
  - **Deletion anomaly:**  
delete all employees with rating 5  
⇒ lose information about the wage for rating 5!

| S           | N         | L  | R | W  | H  |
|-------------|-----------|----|---|----|----|
| 123-22-3666 | Attishoo  | 48 | 8 | 10 | 40 |
| 231-31-5368 | Smiley    | 22 | 8 | 10 | 30 |
| 131-24-3650 | Smethurst | 35 | 5 | 7  | 30 |
| 434-26-3751 | Guldu     | 35 | 5 | 7  | 32 |
| 612-67-4134 | Madayan   | 35 | 8 | 10 | 40 |

Wages

Hourly\_Emps2

| R | W  |
|---|----|
| 8 | 10 |
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*Will 2 smaller tables be better?*

# Normal Forms & Functional Dependencies

- normal forms avoid / minimize certain kinds of problems
  - helps to decide on decomposing relation
- Role of FDs in detecting redundancy
  - No FDs hold: no redundancy
  - Given relation R with 3 attributes ABC and FD  $A \rightarrow B$ :  
Several tuples might have the same A value; if so, they **all have the same B value**

*It's all about hidden repeating information across tuples*

# First Normal Form

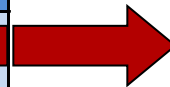
## ■ First Normal Form (1NF)

- eliminates attributes containing sets = **repeating groups**
- ...by flattening: introduce separate tuples with atomic values

■ Ex:

| id | name | skillsList        |
|----|------|-------------------|
| 1  | Jane | {C,C++,SQL}       |
| 2  | John | {Java,python,SQL} |

- Skills not f.d. on id, nor name!



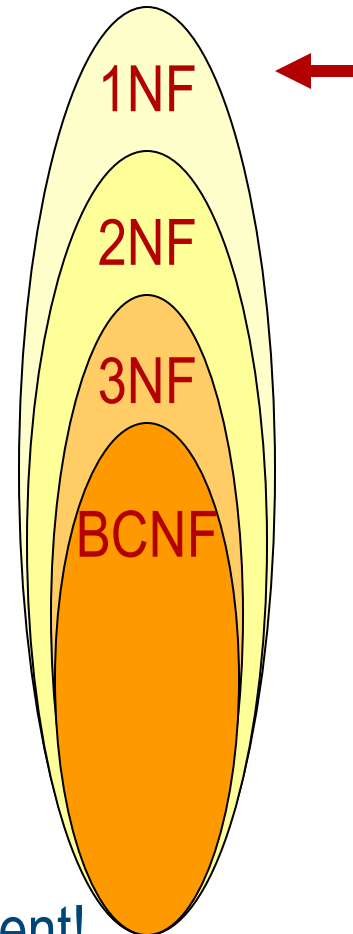
| id | name | skill  |
|----|------|--------|
| 1  | Jane | C      |
| 1  | Jane | C++    |
| 1  | Jane | SQL    |
| 2  | John | Java   |
| 2  | John | Python |
| 2  | John | SQL    |

## ■ Oops: lost primary key property.

- Will fix that later.

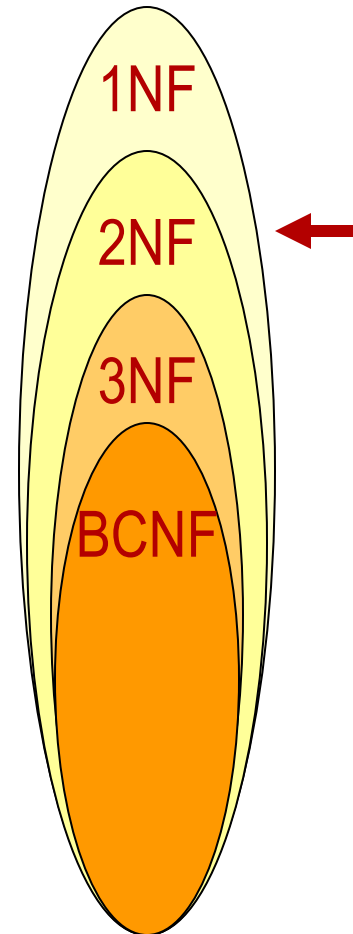
## ■ Why good? Repeating groups complicate storage management!

- Experimental DBMSs exist for non-1NF (NFNF, NF<sup>2</sup>) tables



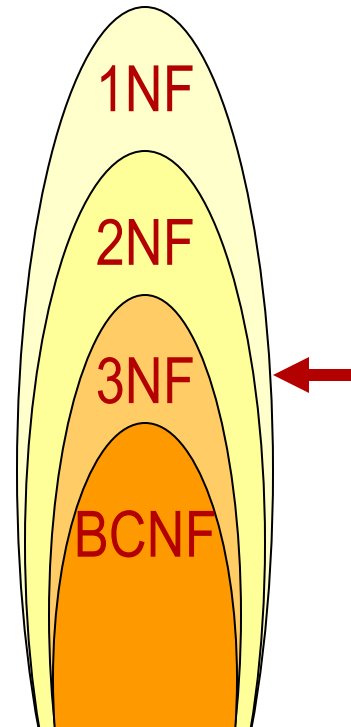
# Second Normal Form

- Second Normal Form (2NF):
  - eliminates functional dependencies on a partial key
  - by putting the fields in a separate table from those that are dependent on the whole key
- Ex: ABCD with  $B \rightarrow C$   
becomes: ABD, BC



# Third Normal Form (3NF)

- Relation R with FD set F is in **3NF** if, for all  $X \rightarrow A$  in  $F^+$ ,
  - Either  $A \in X$  (called a *trivial* FD)
  - Or X contains a key for R
  - Or A is part of some key for R
- In plain words:
  - 3NF eliminates functional dependencies on non-key fields by putting them in a separate table
  - = in 3NF, all non-key fields are dependent on *the key, the whole key, and nothing but the key*
  - Ex:



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# Why Is 3NF Good?

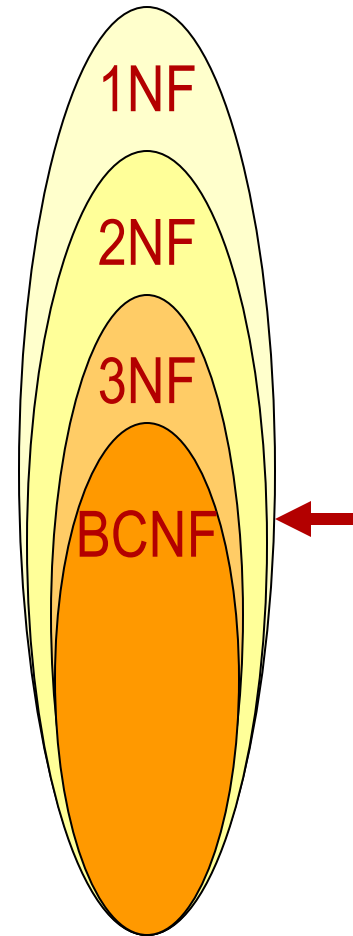
- If 3NF **violated** by  $X \rightarrow A$ , one of the following holds:
- $X$  subset of some key  $K$ 
  - We store  $(X, A)$  pairs **redundantly**
- $X$  not a proper subset of any key
  - Which means: for some key  $K$ , there is a chain of FDs  $K \rightarrow X \rightarrow A$
  - Which means: we once introduced keys to capture dependencies, but now we have **attributes dependent on a non-key attribute!**
- ...so **non-3NF** means **dangerous updates!**

# What Does 3NF **NOT** Achieve?

- Some redundancy possible with 3NF
- Ex: Reserves SBDC,  $S \rightarrow C$ ,  $C \rightarrow S$ 
  - is in 3NF
  - but  $S \leftrightarrow C$  means:  
for each reservation of sailor  $S$ , same  $(S, C)$  pair is stored
- ...so we still need to capture "nests" **inside** the keys

# Boyce-Codd Normal Form (BCNF)

- Relation  $R$  with FDs  $F$  is in **BCNF** if, for all  $X \rightarrow A$  in  $F^+$ ,
  - Either  $A \in X$  (called a *trivial* FD)
  - Or  $X$  contains a key for  $R$
  - ~~• Or  $A$  is part of some key for  $R$~~
  
- In other words:  
 $R$  in BCNF  $\Leftrightarrow$  only key-to-nonkey constraints FDs left
  - ✓ = No redundancy in  $R$  that can be detected using FDs alone
  - ✓ = No FD constraints "hidden in data"



# Discussion: 3NF vs. BCNF

- Always possible?
  - 3NF **always possible**, is “nice” (lossless-join, dependency-preserving)
  - BCNF **not always possible**
- 3NF compromise used when BCNF not achievable
  - Ex: performance considerations
  - Ex: cannot find “good” decomp (see next)

# Decomposition of a Relation Scheme

- Given relation  $R$  with attributes  $A_1 \dots A_n$
- **decomposition** of  $R$  = replacing  $R$  by two or more relations such that:
  - Each new relation scheme contains a subset of the attributes of  $R$  (and no additional attributes), and
  - Every attribute of  $R$  appears as an attribute of one of the new relations
- E.g., decompose SNLRWH into SNLRH and RW

# Example Decomposition

- SNLRWH has FDs  
 $S \rightarrow \text{SNLRWH}$ ,  $R \leftrightarrow W$ ,  $N \rightarrow \text{SN}$
- 2<sup>nd</sup> FD causes **3NF violation**:  
W values repeatedly associated with R values (and vice versa)!
- Easiest fix: create relation RW to store assoc w/o dups, remove W from main schema  
= **decompose** SNLRWH into SNLRH and RW

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Wages

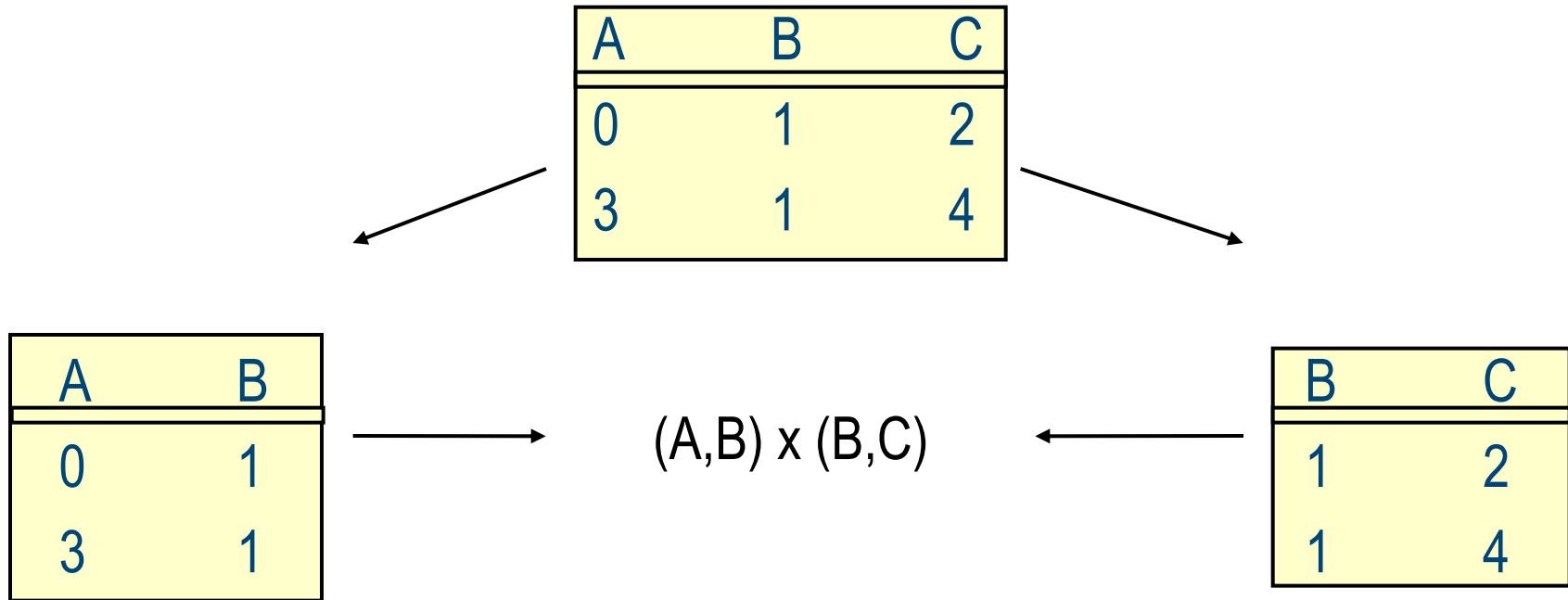
Hourly\_Emps2

| R | W  |
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*If we just store projections of SNLRWH tuples onto SNLRH and RW, are there any potential problems?*

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# Lossless Join: A Counter Example



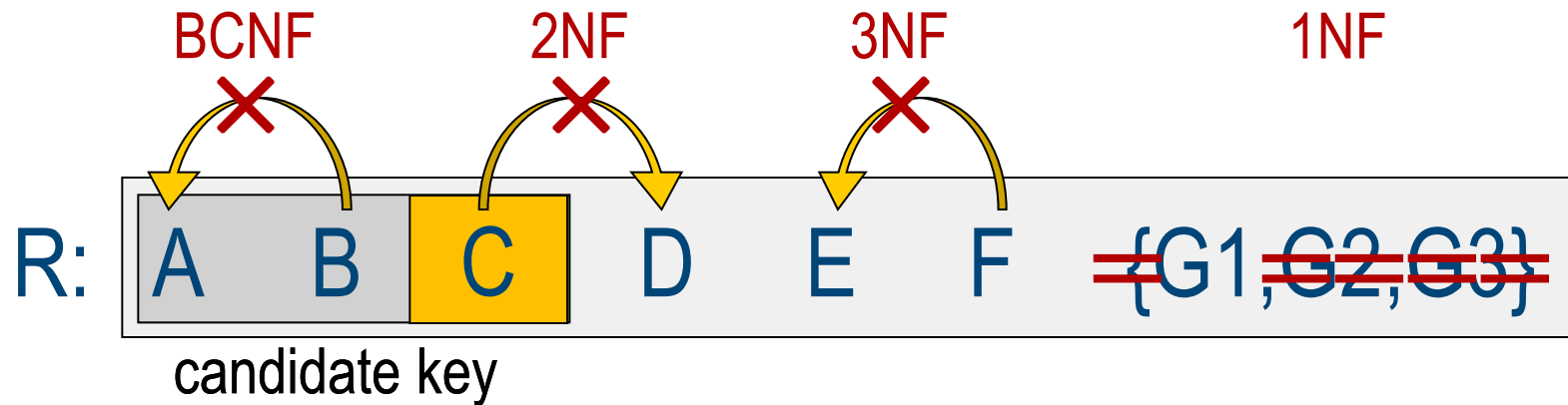
What's wrong?

# Summary of Schema Refinement

- BCNF = free of redundancies that can be detected using FDs
  - BCNF good heuristic (consider typical queries!)
    - *Check FDs !*
  - Next best: 3NF
- When not BCNF?
  - not always possible
  - unsuitable, given typical queries - performance requirements
- Use decompositions only when needed!

 NF pocket guide

# Pocket Guide to NFs



- 1NF = no repeating groups
- 2NF = 1NF + no partial key  $\rightarrow$  non-key
- 3NF = 2NF + no non-key  $\rightarrow$  anything
- BCNF = 3NF + no key  $\rightarrow$  key

## Normalization of table R with FD set :

- For all FDs  $F = „X \rightarrow Y“$ :
  - Create additional table  $R_F(X,Y)$
  - Remove Y from R, but keep X
- Drop duplicate tables arising from „ $X \rightarrow Y, Y \rightarrow X$ “ cycles
- Crosscheck all new tables created against all FDs for decomposition need

# Example Schemas

Contracts (Cid, Sid, Jid, Did, Pid, Qty, Val)  
 Depts (Did, Budget, Report)  
 Suppliers (Sid, Address)  
 Parts (Pid, Cost)  
 Projects (Jid, Mgr)

- Contracts = CSJDPQV; ICs: JP  $\rightarrow$  C, SD  $\rightarrow$  P; C is primary key
  - candidate keys for CSJDPQV?
  - What normal form is this relation schema in?